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**Demographic
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Methods of Estimating Contraceptive Prevalence Rates for Small Areas

**Applications in The Dominican
Republic and Kenya**

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**Demographic and Health Surveys
Methodological Report No. 3**

**Methods of Estimating
Contraceptive Prevalence Rates
for Small Areas: Applications
in The Dominican Republic
and Kenya**

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1 Introduction

Although direct estimates are generally used to determine contraceptive prevalence rates at the national level, such estimates are often unreliable for small areas because the samples are of insufficient size to be representative. Increasingly, however, program managers and policymakers in developing countries have expressed interest in obtaining estimates of basic demographic indicators for small areas in order to set targets, allocate resources, and monitor the performance of family planning and maternal and child health programs (Muhuri and Rutstein, 1994).

Conducting nationally representative DHS surveys in countries that include geographical areas containing small populations is possible, however, it may not be cost-effective. In addition, non-sampling errors may increase with increased sample size. One solution to these problems is to rely on indirect methods to generate estimates for small population areas. This paper examines the suitability of two methods for calculating indirect es-

timates—the *synthetic* estimation procedure and the *regression-based* procedure. Described herein is the estimating equation and the application of each method to the Dominican Republic and Kenya. These two countries were selected because DHS surveys had already been carried out and the samples available were relatively large (IEDP, ONAPLAN, and IRD, 1992; NCPD and IRD, 1989). It is possible, therefore, to compare *direct* estimates with the estimates derived from using the two indirect methods.

Estimates of contraceptive prevalence rates are provided for 30 provinces of the Dominican Republic and 32 districts of Kenya using the *synthetic* and *regression* methods. These are then compared with the results from the *direct* estimation procedure. It was found, after carrying out this comparison, that the *regression* approach is more suitable than the *synthetic* approach as an indirect method for estimating the prevalence of contraceptive use.

2 Definition of a Small Area

In the context of the DHS surveys, a *small area* is defined as a geographical administrative division that has a relatively small population and, therefore, has a corresponding sample size that is too small to provide accurate estimates of demographic parameters. In general, DHS provides estimates of basic demographic parameters, including contraceptive prevalence, that pertain to the nation as a whole, to urban and rural areas, and to the major regions of the country. Administrative divisions smaller than major regions are not usually adequately represented in the surveys.

For the 1991 DHS survey, the Dominican Republic was divided into 8 regions consisting of 30 provinces (see Figure 2.1). The census enumeration area is the primary sampling unit (PSU). The sample included 396 PSUs; at least 40 PSUs were selected from each region. Kenya is divided into 8 provinces which contain 41 districts (see Figure 2.2). However, the 1989 Kenya DHS survey included only 34 districts in 7 provinces covering about 95 percent of the population. As in the Dominican Republic, the census enumeration area in Kenya is the PSU. From each of the seven

provinces, at least 40 PSUs were selected. In both countries, the samples were selected in two stages. In the first stage, PSUs were systematically selected with probability proportional to size (the size equals the number of households in the PSU). In the second stage following an operation to list all households in each selected PSU, individual households were selected with the probability of selection inversely proportional to the PSU's size. This procedure is used in order to maintain a self-weighting sample within major sampling domains.¹ The sample of selected households in each PSU is called a *cluster*.

Provinces in the Dominican Republic and *districts* in Kenya are designated as small areas in this analysis. The goal of this exercise is to obtain estimates of the contraceptive prevalence rates for small areas, i.e., administrative geographical areas (districts/provinces) in which samples were not representative.

¹ For a detailed explanation of the procedure see the *DHS Sampling Manual* (Institute for Resource Development, 1987).

Figure 2.1 Map of the Dominican Republic showing regions and provinces, 1991

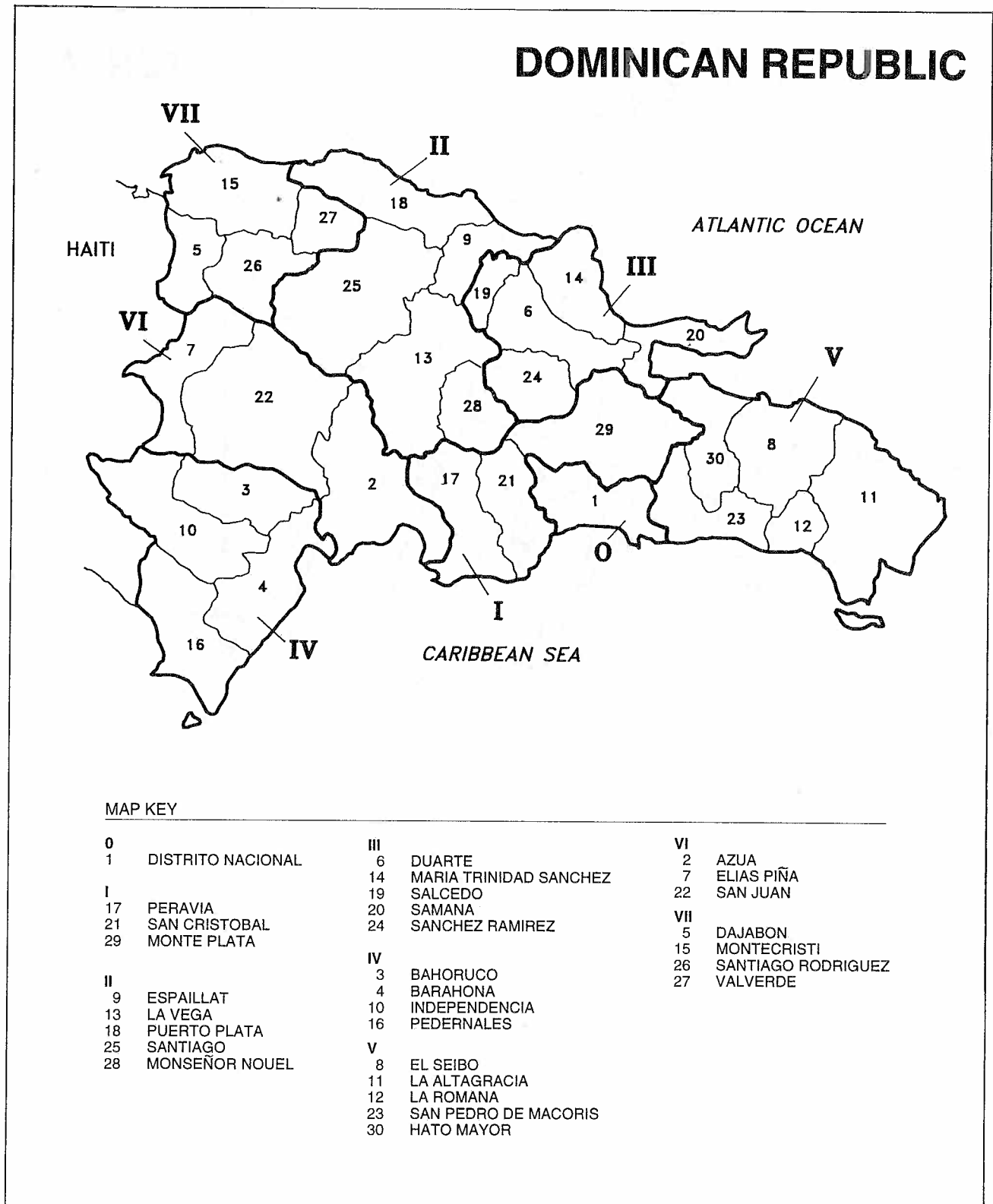
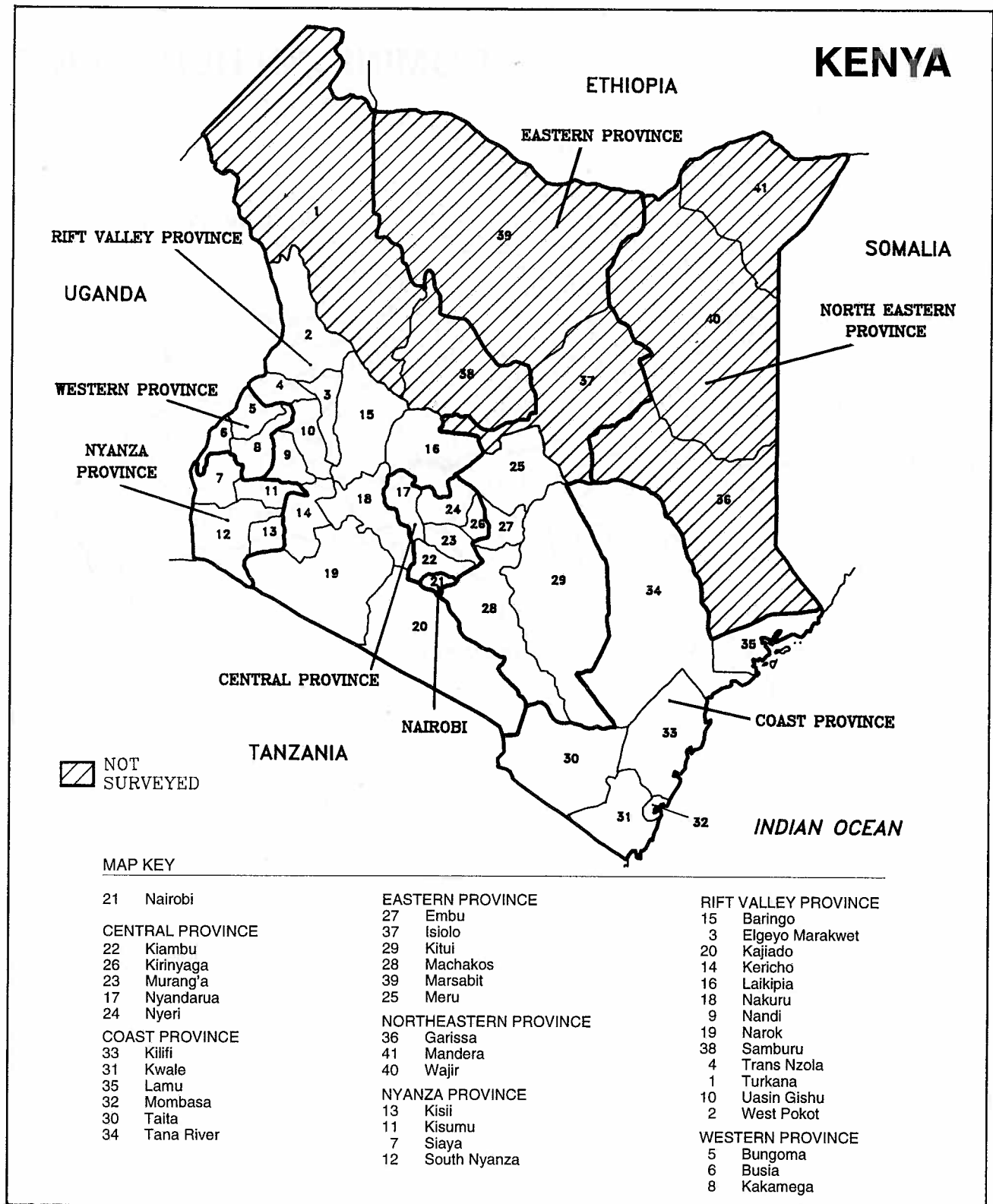


Figure 2.2 Map of Kenya showing provinces and districts, 1989



3 Direct Estimation

The contraceptive prevalence rate is defined as the percentage of married women age 15-49 who are currently using any contraceptive method. It is the ratio of the weighted number of women who are using contraception in an area to the weighted number of married women age 15-49. The formula for *direct estimation* of the contraceptive prevalence rate, r , is as follows:

$$r = \frac{\sum_{i=1}^n w_i y_i}{\sum_{i=1}^n w_i x_i}$$

where:

- r = the contraceptive prevalence rate in a given administrative area;
- w_i = the sampling weight for the i th woman;
- y_i = whether the i th woman is using contraception currently (1 for yes and 0 for no);
- x_i = the counting variable whose value is 1 for every currently married woman;
- n_i = the number of currently married women in the given administrative area.

The procedure is simple, but suitable *only* if the sample size is large. Using this *direct* procedure, the contraceptive prevalence rate is estimated for 7 regions and 30 provinces of the Dominican Republic and 8 provinces and 32 districts of Kenya. The sampling error, which is the square root of the sampling variance, and the relative error, which is the ratio of the sampling error to the estimate² (converted into percentages), are computed for regions and provinces in the Dominican Republic and for provinces and districts in Kenya. Sampling errors and relative errors were not

calculated for 12 provinces of the Dominican Republic and for 14 districts of Kenya. Each of these units had fewer than 9 primary sampling units (PSUs) and, consequently, insufficient degrees of freedom for calculation of the sampling error.

The consistency of the direct estimates was tested by repeatedly calculating prevalence rates based on a varying number of PSUs within a province/district.

In the Dominican Republic, all provinces other than Distrito Nacional have fewer than 30 PSUs. The regional estimates, if they are based on more than 40 PSUs, seem to be reasonable (the larger the number of PSUs in the area, the better the estimate), with relative errors less than 7 percent; the only exception is Region VI for which the relative error of the estimate is 14 percent (see Table 3.1). The estimate for Distrito Nacional, with 65 PSUs, which is the only province under Region 0, is fairly consistent. Estimates for the four provinces which are based on 20-30 PSUs are in the critical region, meaning that they are close to being reasonable but do not have enough consistency. The relative error of those provinces ranges from 5 to 24 percent.

For Kenya, the province- and district-level estimates and other statistics are presented in Table 3.2. As in the Dominican Republic, the province-level prevalence estimates are consistent (the larger the number of PSUs in the area, the better the estimate), if they are based on more than 40 PSUs. Their relative errors range from 5 to 10 percent except for the Western province (15.9). There are 13 districts with 20 to 30 PSUs. The relative errors range from 4 to 23 percent (see Table 3.2).

From the analysis thus far, it was concluded that contraceptive prevalence rates for small areas that have more than 40 PSUs, estimated using the *direct* approach, yield fairly consistent rates.

² Sampling errors were calculated using CLUSTERS software.

Table 3.1 Direct estimates of contraceptive prevalence for married women: Dominican Republic, 1991

Region and province	Direct Estimate (r)	Sampling error (SE)	Relative error (SE/r)	Number of PSUs (m)	Number of cases	
					Unweighted (N)	Weighted (NW)
Region 0	60.7	2.0	3.3	65	688	1450
Distrito Nacional	60.7	2.0	3.3	65	688	1450
Region I	50.8	2.9	5.8	48	471	250
Peravia	48.7	5.8	11.9	14	134	86
San Cristóbal	55.9	3.7	6.6	23	243	112
Monte Plata	43.1	3.9	9.0	11	94	52
Region II	61.0	2.1	3.5	63	643	749
Santiago	62.1	3.5	5.7	29	289	327
Puerto Plata	62.8	5.3	8.5	10	99	102
La Vega	59.4	4.4	7.3	10	108	180
Españillat	56.2	a	a	7	70	58
Monseñor Nouel	61.7	a	a	7	77	82
Region III	57.4	3.7	6.5	50	567	392
Salcedo	53.4	a	a	7	77	45
Duarte	57.2	4.5	7.9	19	220	101
María T. Sánchez	65.9	7.5	11.4	10	105	70
Samaná	44.6	a	a	5	53	21
Sanchez Ramirez	56.7	8.2	14.5	9	112	155
Region IV	47.1	2.7	5.8	41	430	174
Barahona	51.9	2.7	5.1	21	226	88
Pedernales	48.3	a	a	3	32	15
Bahoruco	38.8	6.5	16.8	11	104	48
Independencia	44.8	a	a	6	68	23
Region V	50.6	3.4	6.7	45	524	730
La Romana	44.0	7.9	17.9	12	171	241
La Altagracia	57.5	a	a	7	86	106
El Seybo	46.5	a	a	7	79	116
San P. de Macorís	54.2	3.5	6.4	13	135	174
Hato Mayor	58.0	a	a	6	53	93
Region VI	39.7	5.7	14.4	43	491	193
San Juan	34.1	8.2	24.0	22	236	106
Azua	52.3	4.5	8.6	15	183	62
Elías Piña	32.1	a	a	6	72	25
Region VII	58.6	2.8	4.8	41	412	146
Valverde	53.9	2.4	4.5	15	143	57
Santiago Rodriguez	73.6	a	a	7	63	22
Dajabón	51.8	a	a	7	78	30
Monte Cristi	62.8	4.4	7.1	12	128	37
TOTAL	56.4	1.2	2.1	396	4226	4083

^a Sampling errors not calculated because fewer than 9 PSUs.

Table 3.2 Direct estimates of contraceptive prevalence for married women: Kenya, 1989

Province and district	Direct Estimate (r)	Sampling error (SE)	Relative error (SE/r)	Number of PSUs (m)	Number of cases	
					Unweighted (N)	Weighted (NW)
NAIROBI	33.5	2.1	7.6	40	519	335
CENTRAL	39.5	1.7	5.7	84	787	648
Kiambu	37.3	a	a	5	61	134
Kirinyaga	54.2	3.2	7.2	25	236	88
Murang'a	32.1	5.4	16.7	25	217	162
Nyandarua	39.2	a	a	4	30	83
Nyeri	40.8	3.2	8.7	25	243	181
COAST	18.1	1.7	8.9	47	529	350
Kilifi	10.8	1.7	19.4	24	330	125
Kwale	16.2	a	a	3	34	91
Mombasa	24.5	3.6	17.3	16	147	95
Taita	30.7	a	a	4	18	39
EASTERN	40.2	2.1	7.3	52	561	804
Embu	47.2	a	a	3	27	79
Kitui	41.3	a	a	3	59	186
Machakos	40.4	2.9	7.9	24	282	337
Meru	36.3	3.5	11.6	22	193	202
NYANZA	13.8	1.2	6.3	85	895	872
Kisii	21.5	2.6	11.3	25	245	218
Kisumu	17.8	2.8	6.5	9	194	255
Siaya	8.5	2.2	22.9	25	166	134
South Nyanza	6.1	1.4	16.9	26	290	265
RIFT VALLEY	29.6	1.7	10.5	76	742	1047
Baringo	12.5	a	a	2	16	51
Elgeyo Marak	16.7	a	a	2	12	38
Kajiado	52.0	a	a	2	25	80
Kericho	24.1	2.6	12.0	26	277	205
Laikipia	68.5	a	a	3	25	57
Nakuru	47.2	5.4	3.7	9	88	156
Nandi	16.7	a	a	2	30	95
Narok	22.6	a	a	2	31	99
Trans Nzoia	28.9	a	a	2	45	144
Uasin Gishu	13.4	2.5	19.8	24	180	80
West Pokot	0.0	a	a	2	13	42
WESTERN	13.7	1.3	15.9	54	745	711
Bungoma	9.4	1.5	17.8	26	359	185
Busia	16.1	a	a	3	51	119
Kakamega	14.9	2.0	13.4	25	335	407
TOTAL	26.9	1.0	3.6	438	4778	4765

^a Sampling errors not calculated because fewer than 9 PSUs.

4 Synthetic Estimation

One of the drawbacks of the direct method just described is that the estimate is affected by the large sampling error if the sample size is small. This problem, in turn, inhibits comparison of estimates between areas. One of the ways to overcome the problem of small sample size is to use the proportion of married women from an external source such as a census or a large survey as an adjustment weight. In the literature, several methods of *synthetic estimation* have been discussed (see Aliaga and Le, 1991). The standard synthetic estimation procedure, as suggested in Gonzalez (1973) is used here. The method assumes that the estimated rate is constant within larger areas. What is different between the larger area and the smaller areas within it is the proportion of individuals in the smaller area who have a selected characteristic that is related to the estimate. In other words, in the case of contraceptive prevalence all of the variation in the estimate across the small areas is assumed to be due to differential composition of the populations, not a differential propensity to use contraception. The standard synthetic estimation procedure can be expressed as follows:

$$P_i = \sum_j \left(\frac{N_{ij}}{N_i} \times p_j \right)$$

where:

P_i = the estimated contraceptive prevalence rate in the i th administrative area;

p_j = the observed prevalence rate in the j th auxiliary category;

N_{ij} = the estimated number of married women age 15-49 in the j th auxiliary category for the i th area, as observed in the external source;

N_i = the estimated number of married women age 15-49 in the i th area, as observed in the external source; and

N_{ij}/N_i = the adjustment weights.

Contraceptive use age patterns were examined for the Dominican Republic and Kenya. The results indicate that the contraceptive prevalence rate increases with an increase in women's age, par-

ticularly from age group 15-19 to age group 35-39. Logistic regression analysis also shows that the log odds of contraceptive use are higher for women who are age 25-34 and 35-49 than for those women who are in the 15-24 age group. Since a woman's age is an important predictor of contraceptive use and data on women's age are available from an external source, it was decided to use women's age as a weighting factor in the estimation of the prevalence rate for small population areas. Data on women's age as an auxiliary variable are taken from the 1991 15,000-household survey for the Dominican Republic and from the 1990 Population Census for Kenya.

The distribution of married women in the three age groups (15-24, 25-34, and 35-49) within each province/district was calculated. Homogeneity of prevalence rates is assumed for each age group within the region/province. The estimates produced by the synthetic method are presented in Table 4.1 for the Dominican Republic and in Table 4.2 for Kenya.

Monte Plata (in Region I) in the Dominican Republic is used as an example to show how the calculation is performed. The adjustment weights (N_{ij}/N_i) are computed from the auxiliary age data as .29, .32, and .40 for age groups 15-24, 25-34, and 35-49, respectively; the region-level contraceptive prevalence rates are .288, .627, and .590, respectively, for the three age groups. Using the above formula, we estimate the contraceptive prevalence rate as 51.4 percent for the Monte Plata province: $(.29 \times .288) + (.32 \times .627) + (.40 \times .590)$.

In this calculation, the assumption is made that the provinces/districts within the region/province are homogeneous with respect to age-specific contraceptive prevalence rates. Even if the assumption of homogeneity is not correct, any possible extreme estimate is brought in line with the regional estimate. It is observed from Table 4.1, that the province-level estimates are close to regional estimates for the Dominican Republic. A similar situation occurs among districts in Kenya (see Table 4.2), although dissimilarities are stronger among provinces in Kenya than among regions in the Dominican Republic. Because of the fact that the sampling frame for the auxiliary age variable is different from that for the contraceptive use variable, the sampling variance of the synthetic estimate has not been calculated.

Table 4.1 Synthetic estimates of contraceptive prevalence for married women: Dominican Republic 1991

Region and province	Distribution of married women by age ¹			Total percent	Regional contraceptive prevalence rate and relative error ²				Synthetic estimate of contraceptive prevalence
	15-24	25-34	35-49		15-24 (RE)	25-34 (RE)	35-49 (RE) ³	15-49	
REGION 0					36.0 (14.4)	60.8 (5.3)	73.2 (4.0)	60.7	
D. Nacional	20.0	41.2	38.8	100.0					60.6
REGION I					28.8 (15.1)	62.7 (5.6)	59.0 (6.0)	50.8	
Peravia	28.8	32.1	39.2	100.0					51.5
San Cristobal	22.2	37.4	40.5	100.0					53.7
Monte Plata	28.9	31.5	39.7	100.0					51.4
REGION II					42.3 (11.0)	67.0 (4.5)	70.0 (5.4)	61.0	
Santiago	24.6	37.0	38.5	100.0					62.1
Puerto Plata	24.2	43.0	32.9	100.0					62.0
La Vega	26.5	38.9	34.6	100.0					61.5
Españillat	24.7	40.0	35.4	100.0					62.0
Monseñor Nouel	28.0	37.2	34.9	100.0					61.2
REGION III					39.0 (19.1)	65.7 (10.0)	60.2 (6.7)	57.4	
Salcedo	25.0	39.9	35.2	100.0					57.1
Duarte	27.9	33.6	38.6	100.0					56.1
M. T. Sanchez	22.3	40.9	36.9	100.0					57.8
Samana	31.4	26.9	41.8	100.0					55.0
S. Ramirez	19.3	43.3	37.4	100.0					58.5
REGION IV					26.4 (15.6)	56.9 (6.1)	56.1 (8.5)	47.1	
Barahona	28.5	31.8	39.8	100.0					47.9
Pedernales	38.0	37.2	24.8	100.0					45.1
Bahoruco	29.3	36.9	33.9	100.0					47.7
Independencia	31.5	28.3	40.3	100.0					46.2
REGION V					33.5 (13.5)	51.1 (8.4)	66.0 (7.2)	50.6	
La Romana	31.1	39.5	29.5	100.0					50.1
La Altagracia	28.7	35.5	35.9	100.0					51.4
El Seibo	28.3	38.9	32.9	100.0					51.0
S. P. Macoris	24.2	38.8	37.0	100.0					52.3
Hato Mayor	23.2	43.5	33.3	100.0					51.9
REGION VI					22.8 (27.3)	46.8 (10.0)	45.1 (17.4)	39.7	
San Juan	27.8	36.6	35.6	100.0					39.5
Azua	29.6	33.9	36.5	100.0					39.0
Elías Piña	26.0	33.0	41.1	100.0					39.9
REGION VII					26.2 (16.6)	74.3 (7.3)	65.3 (7.9)	58.6	
Valverde	24.2	36.6	39.3	100.0					59.1
S. Rodriguez	15.5	38.6	45.9	100.0					62.7
Dajabon	29.9	32.9	37.2	100.0					56.5
Monte Cristi	30.3	30.6	39.2	100.0					56.3

Note: Values in parentheses indicate relative errors.

¹1991 Expanded Household Survey (IEPD, ONAPLAN, and MI, 1993)

²1991 DHS survey (IEPD, ONAPLAN, and IRD, 1992)

³See Table 3.1 for relative error

Table 4.2 Synthetic estimates of contraceptive prevalence for married women: Kenya, 1989

Province and district	Distribution of married women by age ¹			Total percent	Regional contraceptive prevalence rate and relative error ²				Synthetic estimate of contraceptive prevalence
	15-24	25-34	35-49		15-24 (RE)	25-34 (RE)	35-49 (RE) ³	15-49	
NAIROBI					19.1 (15.9)	39.2 (10.0)	49.1(8.5)	33.5	
Nairobi	32.7	44.8	22.5	100.0					34.9
CENTRAL					28.2 (21.6)	39.1(7.0)	45.2(8.9)	39.5	
Kiambu	27.1	40.1	32.8	100.0					38.1
Kirinyaga	25.1	39.5	35.4	100.0					38.5
Murang'a	21.6	38.8	39.5	100.0					39.2
Nyandarua	26.8	37.6	35.6	100.0					38.4
Nyeri	22.3	38.9	38.8	100.0					39.0
COAST					6.9 (39.7)	23.9 (12.5)	18.6 (20.8)	18.1	
Kilifi	29.3	37.8	32.9	100.0					17.2
Kwale	30.7	38.2	31.1	100.0					17.0
Mombasa	32.5	42.2	25.4	100.0					17.0
Taita	22.4	39.1	38.4	100.0					18.1
EASTERN					32.4 (13.0)	43.6(8.8)	40.5(9.8)	40.2	
Embu	21.9	41.0	37.2	100.0					40.0
Kitui	25.1	36.4	38.5	100.0					39.6
Machakos	21.6	40.3	38.1	100.0					40.0
Meru	22.8	41.4	35.8	100.0					39.9
NYANZA					9.9 (24.5)	13.9(9.0)	16.2 (15.4)	13.8	
Kisii	27.9	42.2	30.0	100.0					13.5
Kisumu	31.4	38.7	29.9	100.0					13.3
Siaya	26.5	35.5	38.0	100.0					13.7
South Nyanza	34.6	36.4	29.0	100.0					13.2
RIFT VALLEY					25.6 (20.9)	30.2 (12.9)	31.4 (17.2)	29.6	
Baringo	26.5	40.6	33.0	100.0					29.4
Elgeyo Marak	26.5	39.2	34.3	100.0					29.4
Kajiado	38.1	36.3	25.6	100.0					28.8
Kericho	31.7	39.3	29.1	100.0					29.1
Laikipia	26.6	39.1	34.3	100.0					29.4
Nakuru	30.5	39.9	29.6	100.0					29.2
Nandi	28.1	39.1	32.8	100.0					29.3
Narok	37.4	36.5	26.1	100.0					28.8
Trans Nzoia	29.8	39.8	30.5	100.0					29.2
Uasin Gishu	29.7	40.1	30.2	100.0					29.2
West Pokot	32.7	37.5	29.8	100.0					29.1
WESTERN					5.7 (32.0)	15.6 (20.8)	17.6 (18.9)	13.7	
Bungoma	30.7	39.6	29.7	100.0					13.2
Busia	30.9	37.4	31.7	100.0					13.2
Kakamega	U	U	U	U					U

Note: Values in parentheses indicate relative errors.

U=Unknown (not available)

¹1990 Population Census

²1989 DHS survey (NCPD and IRD, 1989)

³See Table 3.2 for relative error

5 Regression Method

One of the main weaknesses of the synthetic method is that only a few auxiliary variables can be used at a time. Another problem is that the sampling and nonsampling errors of the auxiliary variables from the external source are not compatible with those of the prevalence estimates from the main source. Using the *regression approach* alleviates these problems. The regression method includes all the potential predictors related to current use of contraception, while relying only on data from the main source.

The DHS data from both the Dominican Republic and Kenya suggest that use of contraception is associated with a woman's age, education, number of living children, work status, floor type, urban-rural residence, water supply, electricity in the house, possession of a radio, toilet type, and husband's education. These 11 variables are reformulated into 11 dummy variables (1,0), based on the cutoffs determined through a two-step process to maximize the power of discrimination of the predictor (Goldstein and Dillon, 1978). First, the cumulative distribution of each of the predictors is constructed for two subgroups: those who are currently using a family planning method and those who are not. Then, the absolute difference in the cumulative frequency between the two subgroups is calculated for each of the categories of the predictor. The cutoff point, x^* , is that value (or the category) of the original predictor which maximizes the difference in the cumulative frequency between use and nonuse subgroups, which can be expressed as follows:

$$|F_u(x^*) - F_n(x^*)| = \max_x |F_u(x) - F_n(x)|$$

where:

$F_u(x)$ = the cumulative frequency distribution of the original predictor at value x for the use subgroup; and

$F_n(x)$ = the cumulative frequency distribution of the original predictor at value x for the nonuse subgroup.

The 11 predictor dummies and the dummy variable on current contraception (1,0) are constructed at the individual level. The values of these 11 dummies are averaged in order to create a cluster-level numeric variable, expressed in terms of a proportion ($p_1 \dots p_{11}$). Similarly, the values of the contraceptive use dummy are converted into the prevalence rate, P_c , at the cluster level. This is done from cluster 1 to m (where m is the total number of clusters), as shown below. As noted earlier, the cluster is a sample of selected households in each PSU.

Cluster No.	p_1	p_2	...	p_{11}	P_c
1					
2					
3					
4					
.					
.					
.					
m					

The contraceptive prevalence rate is regressed on the 11 factors, with the cluster as the unit of analysis. The regression equation can be expressed as follows:

$$P_c = \alpha_0 + \alpha_1 p_{1c} + \alpha_2 p_{2c} + \dots + \alpha_{11} p_{11c}$$

where:

P_c = the observed prevalence rate in cluster c ($=1, \dots, m$);

α_0 = the intercept;

α_1 = the coefficient for predictor p_1 ;

α_2 = the coefficient for predictor p_2 ;

α_{11} = the coefficient for predictor p_{11} ; and

e_c = the error term for cluster c .

Using the backward selection option of the linear regression procedure in the Statistical Package for Social Sciences (SPSS), the best model is identified. No sampling weights were used in the regression analysis; however, the predicted prevalence rate at the cluster-level estimated from the regression equation is adjusted for sampling weights to produce the final province/district level estimates, using the following formula:

$$P = \frac{\sum b_c w_c P_{pc}}{\sum b_c w_c}$$

where:

P = the prevalence rate at the province/district level;

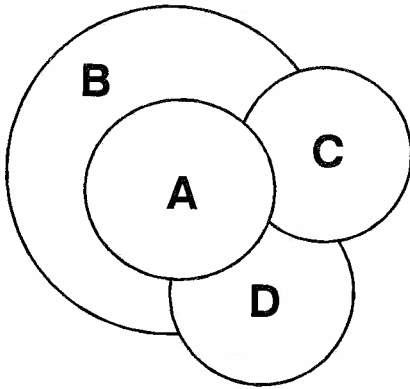
b_c = the number of women in cluster c ;

w_c = the sampling weight for cluster c ;

P_{pc} = the predicted prevalence rate for cluster c ; and

the sum Σ is over all clusters in the given province/district.

If a given province in the Dominican Republic or a district in Kenya has fewer than 30 clusters, several new sets of clusters were formed by adding clusters from the contiguous province/district such that some original clusters remain in each of the new sets. The predicted prevalence rates estimated from the models for the new sets are averaged. This average rate is the final province-level prevalence estimate. This can be illustrated by the following Venn Diagram:



The diagram has four subsets of clusters representing Provinces A, B, C, and D. The objective is to estimate the contraceptive prevalence rate for Province A, which has fewer than 30 clusters. It is necessary to add clusters from the neighboring provinces to meet the required number of at least 30 clusters. There exist at least three possible groupings: A and B; A, C, and D, and A, D, and B and the corresponding prevalence rates are $P(I)$, $P(II)$ and $P(III)$. The estimated rate for Province A is obtained by averaging the three rates.

Three sets of estimates are presented for the Dominican Republic in Table 5.1 and for Kenya in Table 5.2. Note that there are some regions in the Dominican Republic (e.g., Region VI) and some provinces in Kenya (e.g., Rift Valley) which have provincial/district prevalence estimates that vary dramatically. These extreme values have been smoothed out (are brought in line with regional variation) by the regression method. However, the interprovince variability (for the Dominican Republic) or the interdistrict variability (for Kenya) is only slightly reduced compared to the direct estimate. In contrast, the interarea variability in the estimate obtained from the synthetic method is reduced considerably. Tables 5.1 and 5.2 also show that the estimates of the sampling errors in the regression method are, in general, lower than those in the direct method.

Table 5.1 Direct, synthetic, and regression estimates of contraceptive prevalence for married women: Dominican Republic, 1991

Region and province	Direct estimate		Synthetic estimate	Regression estimate	
	Value	Sampling error		Value	Sampling error
REGION 0	60.7				
Distrito Nacional	60.7	2.0	60.6	61.7	1.8
REGION I	50.8				
Peravia	48.7	5.8	51.5	54.6	3.0
San Cristóbal	55.9	3.7	53.7	52.3	2.6
Monte Plata	43.1	3.9	51.4	52.3	3.5
REGION II	61.0				
Santiago	62.1	3.5	62.1	60.7	4.4
Puerto Plata	62.8	5.3	62.0	58.6	2.1
La Vega	59.4	4.4	61.5	58.0	2.0
Españolat	56.2	a	62.0	57.3	3.5
Monseñor Nouel	61.7	a	61.2	56.7	2.0
REGION III	57.4				
Salcedo	53.4	a	57.1	56.1	3.4
Duarte	57.2	4.5	56.1	55.3	2.3
María T. Sánchez	65.9	7.5	57.8	57.9	1.6
Samaná	44.6	a	55.0	57.9	1.6
Sanchez Ramirez	56.7	8.2	58.5	53.7	4.3
REGION IV	47.1				
Barahona	51.9	2.7	47.9	50.0	3.3
Pedernales	48.3	a	45.1	50.0	2.4
Bahoruco	38.8	6.5	47.7	43.4	4.8
Independencia	44.8	a	46.2	49.1	2.5
REGION V	50.6				
La Romana	44.0	7.9	50.1	50.1	4.0
La Altagracia	57.5	a	51.4	49.8	4.1
El Seybo	46.5	a	51.0	49.5	3.4
San P. de Macorís	54.2	3.5	52.3	50.8	3.3
Hato Mayor	58.0	a	51.9	49.6	2.7
REGION VI	39.7				
San Juan	34.1	8.2	39.5	41.5	6.6
Azua	52.3	4.5	39.0	52.7	3.2
Elías Piña	32.1	a	39.9	40.5	8.0
REGION VII	58.6				
Valverde	53.9	2.4	59.1	58.4	2.9
Santiago Rodriguez	73.6	a	62.7	55.1	4.9
Dajabón	51.8	a	56.5	55.8	6.3
Monte Cristi	62.8	4.4	56.3	59.3	2.6

^a Sampling errors not calculated because fewer than 9 PSUs.

Table 5.2 Direct, synthetic, and regression estimates of contraceptive prevalence for married women: Kenya, 1989

Province and district	Direct estimate		Synthetic estimate	Regression estimate	
	Value	Sampling error		Value	Sampling error
NAIROBI					
Nairobi	33.5	2.1	34.9	38.5	3.6
CENTRAL	39.5				
Kiambu	37.3	a	38.1	37.9	3.2
Kirinyaga	54.2	3.2	38.5	44.4	2.0
Murang'a	32.1	5.4	39.2	38.8	2.5
Nyandarua	39.2	a	38.4	40.4	3.2
Nyeri	40.8	3.2	39.0	43.3	2.8
COAST	18.1				
Kilifi	10.8	1.7	17.2	15.2	2.6
Kwale	16.2	a	17.0	17.3	4.3
Mombasa	24.5	3.6	17.0	15.0	2.0
Taita	30.7	a	18.1	29.0	1.9
EASTERN	40.2				
Embu	47.2	a	40.0	42.1	2.4
Kitui	41.3	a	39.6	41.6	2.7
Machakos	40.4	2.9	40.0	41.0	1.7
Meru	36.3	3.5	39.9	43.4	3.8
NYANZA	13.8				
Kisii	21.5	2.6	13.5	16.9	1.4
Kisumu	17.8	2.8	13.3	14.8	1.3
Siaya	8.5	2.2	13.7	10.1	1.5
South Nyanza	6.1	1.4	13.2	11.2	1.0
RIFT VALLEY	29.6				
Baringo	12.5	a	29.4	27.1	3.1
Elgeyo Marak	16.7	a	29.4	15.0	2.8
Kajiado	52.0	a	28.8	41.5	4.6
Kericho	24.1	2.6	29.1	19.3	1.6
Laikipia	68.5	a	29.4	45.0	4.5
Nakuru	47.2	5.4	29.2	34.0	5.2
Nandi	16.7	a	29.3	18.0	2.2
Narok	22.6	a	28.8	23.3	4.5
Trans Nzoia	28.9	a	29.2	15.1	2.5
Uasin Gishu	13.4	2.5	29.2	15.7	2.3
West Pokot	0.0	a	29.1	U	U
WESTERN	13.7				
Bungoma	9.4	1.5	13.2	11.8	1.8
Busia	16.1	a	13.2	11.7	2.2
Kakamega	14.9	2.0	U	14.4	1.7

U=Unknown (data required for estimate were not available)

^a Sampling errors not calculated because fewer than 9 PSUs.

6 Conclusions

The estimates provided by these three methods are consistent (the larger the number of PSUs in the area, the better the estimate). The range of both synthetic and regression estimates for provinces/districts within each region in the Dominican Republic and each province in Kenya is smaller than the range for the direct estimate (see Tables 6.1 and 6.2). For the Dominican Republic, the correlation value between the direct and synthetic provincial estimates is 0.90, 0.88 between the direct and regression provincial estimates, and 0.95 between the synthetic and regression provincial estimates. For the 30 districts in Kenya (excluding West Pokot and Kakamega), the correlation values between district estimates are 0.70, 0.90, and 0.85, respectively. Restricting the analysis to provinces/districts having at least 200 cases yields slightly higher correlation values, supporting the finding that the estimates are consistent. In general, the correlation values are slightly higher for the Dominican Republic than for Kenya, probably due to the fact that provinces in the Dominican Republic are more homogenous than districts in Kenya.

Of the three methods used to estimate contraceptive prevalence rates, the regression approach was found most suitable. First, the

approach overcomes the problem of small numbers of cases encountered in the direct estimation procedure by averaging the estimates of several sets, each of which contains the common areas (provinces of Dominican Republic and districts of Kenya) of interest. Although this could be done with the direct method, there are no objective criteria for selecting which areas should form a set. Such criteria in the regression approach are developed by finding whether the same set of predictors explains the use of contraception in the areas that constitute a set. Second, unlike the synthetic approach, no auxiliary data are needed in the regression approach and the assumption of homogeneity is not required. Third, the regression method allows for estimates of sampling error, while the synthetic procedure does not.

Another possible approach to indirect estimation that is not examined in this report is the empirical Bayes approach (Fay and Herriot, 1979), which would essentially be a weighted average of the direct province/district estimate and the regional/provincial estimate of contraceptive prevalence. This new prevalence estimate gives more weight to the region/province estimate (more accurate) than to the province/district estimate.

Table 6.1 Range of contraceptive prevalence rates among provinces by region, midpoint \pm half range: Dominican Republic, 1991

Region	Direct estimate	Synthetic estimate	Regression estimate
Region I	49.50 \pm 6.40	52.55 \pm 1.15	53.45 \pm 1.15
Region II	59.50 \pm 3.30	61.65 \pm 0.45	58.70 \pm 2.00
Region III	55.25 \pm 10.65	56.75 \pm 1.25	55.80 \pm 2.10
Region IV	45.35 \pm 6.55	46.50 \pm 1.40	46.70 \pm 3.30
Region V	51.00 \pm 7.00	51.20 \pm 1.10	50.15 \pm 0.65
Region VI	42.20 \pm 10.10	39.45 \pm 0.45	46.60 \pm 6.10
Region VII	62.70 \pm 10.90	59.50 \pm 3.20	57.20 \pm 2.10
TOTAL	52.85 \pm 20.75	50.85 \pm 11.85	51.10 \pm 10.60

Table 6.2 Range of contraceptive prevalence rates among districts by province, midpoint \pm half range: Kenya, 1989

Province	Direct estimate	Synthetic estimate	Regression estimate
Central	43.15 \pm 11.05	38.65 \pm 0.55	41.15 \pm 3.25
Coast	20.75 \pm 9.95	17.55 \pm 0.55	22.00 \pm 7.00
Eastern	41.75 \pm 5.45	39.80 \pm 0.20	42.20 \pm 1.20
Nyanza	13.80 \pm 7.70	13.45 \pm 0.25	13.50 \pm 3.40
Rift Valley	40.50 \pm 28.00	29.10 \pm 0.30	30.00 \pm 15.00
Western	12.75 \pm 3.35	13.20 \pm 0.00	13.05 \pm 1.35
TOTAL	37.30 \pm 31.20	26.60 \pm 13.40	27.55 \pm 17.45

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Appendix

Summary of DHS-I and DHS-II Surveys, 1985-1993

Region and Country	Date of Fieldwork	Implementing Organization	Respondents	Sample Size	Male/Husband Survey	Supplemental Studies, Modules, and Additional Questions
SUB-SAHARAN AFRICA						
DHS-I						
Botswana	Aug-Dec 1988	Central Statistics Office	AW 15-49	4,368		AIDS, PC, adolescent fertility
Burundi	Apr-Jul 1987	Département de la Population, Ministère de l'Intérieur	AW 15-49	3,970	542 Husbands	CA, SAI, adult mortality
Ghana	Feb-May 1988	Ghana Statistical Service	AW 15-49	4,488	943 Husbands	CA, SM, WE
Kenya	Dec-May 1988/89	National Council for Population and Development	AW 15-49	7,150	1,133 Husbands	
Liberia	Feb-Jul 1986	Bureau of Statistics, Ministry of Planning and Economic Affairs	AW 15-49	5,239		TBH, employment status
Mali	Mar-Aug 1987	Institut du Sahel, USED/CERPOD	AW 15-49	3,200	970 Men 20-55	CA, VC, childhood physical handicaps
Ondo State, Nigeria	Sep-Jan 1986/87	Ministry of Health, Ondo State	AW 15-49	4,213		CA, TBH
Senegal	Apr-Jul 1986	Direction de la Statistique, Ministère de l'Economie et des Finances	AW 15-49	4,415		CA, CD
Sudan	Nov-May 1989/90	Department of Statistics, Ministry of Economic and National Planning	EMW 15-49	5,860		M, MM, female circumcision, family planning services
Togo	Jun-Nov 1988	Unité de Recherche Démographique, Université du Bénin	AW 15-49	3,360		CA, SAI, marriage history
Uganda	Sep-Feb 1988/89	Ministry of Health	AW 15-49	4,730		CA, SAI
Zimbabwe	Sep-Jan 1988/89	Central Statistical Office	AW 15-49	4,201		AIDS, CA, PC, SAI, WE
DHS-II						
Burkina Faso	Dec-Mar 1992/93	Institut National de la Statistique et de la Démographie	AW 15-49	6,000	1,845 Men 18+	AIDS, CA, MA, SAI
Cameroon	Apr-Sep 1991	Direction Nationale du Deuxième Recensement Général de la Population et de l'Habitat	AW 15-49	3,871	814 Husbands	CA, CD, SAI
Madagascar	May-Nov 1992	Centre National de Recherches sur l'Environnement	AW 15-49	6,260		CA, MM, SAI
Malawi	Sep-Nov 1992	National Statistical Office	AW 15-49	4,850	1,151 Men 20-54	AIDS, CA, MA, MM, SAI
Namibia	Jul-Nov 1992	Ministry of Health and Social Services, Central Statistical Office	AW 15-49	5,421		CA, CD, MA, MM
Niger	Mar-Jun 1992	Direction de la Statistique et des Comptes Nationaux	AW 15-49	6,503	1,570 Husbands	CA, MA, MM, SAI
Nigeria	Apr-Oct 1990	Federal Office of Statistics	AW 15-49	8,781		CA, SAI
Rwanda	Jun-Oct 1992	Office National de la Population	AW 15-49	6,551	598 Husbands	CA, SAI
Senegal	Nov-Aug 1992/93	Direction de la Prévision et de la Statistique	AW 15-49	6,310	1,436 Men 20+	AIDS, CA, MA, MM, SAI
Tanzania	Oct-Mar 1991/92	Bureau of Statistics, Planning Commission	AW 15-49	9,238	2,114 Men 15-60	AIDS, CA, MA, SAI
Zambia	Jan-May 1992	University of Zambia	AW 15-49	7,060		AIDS, CA, MA
NEAR EAST/NORTH AFRICA						
DHS-I						
Egypt	Oct-Jan 1988/89	National Population Council	EMW 15-49	8,911		CA, CD, MM, PC, SAI, WE, women's status
Morocco	May-Jul 1987	Ministère de la Santé Publique	EMW 15-49	5,982		CA, CD, S
Tunisia	Jun-Oct 1988	Office National de la Famille et de la Population	EMW 15-49	4,184		CA, CD, S, SAI
DHS-II						
Egypt	Nov-Dec 1992	National Population Council	EMW 15-49	9,864	2,406 Husbands	CA, MA, PC, SM
Jordan	Oct-Dec 1990	Department of Statistics, Ministry of Health	EMW 15-49	6,462		CA, SAI
Morocco	Jan-Apr 1992	Ministère de la Santé Publique	AW 15-49	9,256	1,336 Men 20-70	CA, MA, MM, SAI
Yemen	Nov-Jan 1991/92	Central Statistical Organization	EMW 15-49	5,687		CA, CD, SAI

Region and Country	Date of Fieldwork	Implementing Organization	Respondents	Sample Size	Male/Husband Survey	Supplemental Studies, Modules, and Additional Questions
ASIA						
DHS-I						
Indonesia	Sep-Dec 1987	Central Bureau of Statistics, National Family Planning Coordinating Board	EMW 15-49	11,844		PC, SM
Nepal (In-depth)	Feb-Apr 1987	New Era	CMW 15-49	1,623		KAP-gap survey
Sri Lanka	Jan-Mar 1987	Department of Census and Statistics, Ministry of Plan Implementation	EMW 15-49	5,865		CA, NFP
Thailand	Mar-Jun 1987	Institute of Population Studies, Chulalongkorn University	EMW 15-49	6,775		CA, S, SAI
DHS-II						
Indonesia	May-Jul 1991	Central Bureau of Statistics, National Family Planning Coordinating Board, Ministry of Health	EMW 15-49	22,909		PC, SM
Pakistan	Dec-May 1990/91	National Institute of Population Studies	EMW 15-49	6,611	1,354 Husbands	CA
LATIN AMERICA & CARIBBEAN						
DHS-I						
Bolivia	Mar-Jun 1989	Instituto Nacional de Estadística	AW 15-49	7,923		CA, CD, MM, PC, S, WE
Bolivia (In-depth)	Mar-Jun 1989	Instituto Nacional de Estadística	AW 15-49	7,923		Health
Brazil	May-Aug 1986	Sociedade Civil Bem-Estar Familiar no Brasil	AW 15-44	5,892		CA, PC, SM, abortion, young adult use of contraception
Colombia	Oct-Dec 1986	Corporación Centro Regional de Población, Ministerio de Salud	AW 15-49	5,329		CA, PC, SAI, SM
Dominican Republic	Sep-Dec 1986	Consejo Nacional de Población y Familia	AW 15-49	7,649		NFP, S, SAI, SM family planning communication
Dominican Rep. (Experimental)	Sep-Dec 1986	Consejo Nacional de Población y Familia	AW 15-49	3,885		
Ecuador	Jan-Mar 1987	Centro de Estudios de Población y Paternidad Responsable	AW 15-49	4,713		CD, SAI, employment
El Salvador	May-Jun 1985	Asociación Demográfica Salvadoreña	AW 15-49	5,207		S, TBH
Guatemala	Oct-Dec 1987	Instituto de Nutrición de Centro América y Panamá	AW 15-44	5,160		S, SAI
Mexico	Feb-May 1987	Dirección General de Planificación Familiar Secretaría de Salud	AW 15-49	9,310		NFP, S, employment
Peru	Sep-Dec 1986	Instituto Nacional de Estadística	AW 15-49	4,999		NFP, employment, cost of family planning
Peru (Experimental)	Sep-Dec 1986	Instituto Nacional de Estadística	AW 15-49	2,534		
Trinidad and Tobago	May-Aug 1987	Family Planning Association of Trinidad and Tobago	AW 15-49	3,806		CA, NFP, breastfeeding
DHS-II						
Brazil (NE)	Sep-Dec 1991	Sociedade Civil Bem-Estar Familiar no Brasil	AW 15-49	6,222	1,266 Husbands	AIDS, PC
Colombia	May-Aug 1990	PROFAMILIA	AW 15-49	8,644		AIDS
Dominican Republic	Jul-Nov 1991	Instituto de Estudios de Población y Desarrollo (PROFAMILIA), Oficina Nacional de Planificación	AW 15-49	7,320		CA, MA, S, SAI
Paraguay	May-Aug 1990	Centro Paraguayo de Estudios de Población	AW 15-49	5,827		CA, SAI
Peru	Oct-Mar 1991/92	Instituto Nacional de Estadística e Informática	AW 15-49	15,882		CA, MA, MM, SAI

AW all women

CMW currently married women

EMW ever-married women

AIDS acquired immune deficiency syndrome

CA child anthropometry

CD causes of death (verbal reports of symptoms)

M migration

MA maternal anthropometry

MM maternal mortality

NFP natural family planning

PC pill compliance

S sterilization

SAI service availability information

SM social marketing

TBH truncated birth history

VC value of children

